

# VCE Algorithmics (HESS)

## Written examination – End of year

### Sample questions

#### SECTION A – Multiple-choice questions

##### Question 1

Consider the following pseudocode, written by Cecily, an Algorithmics student.

```
Algorithm MakeChange
    Input: T, integer, total amount of change to be given
    Output: 1-D array, a set of coins to make a total of T

    Let L = an array of coin values in reverse sorted order
    Let finalList = an empty array

    for eachValue in L
        count = ( T / eachValue ) rounded down
        Append eachValue to the end of finalList
        T = T - ( eachValue*T )
    endfor
    return finalList
```

Cecily is checking the pseudocode to solve the change making problem. She uses the following values:

- L = [50, 20, 10, 5, 1]
- T = 175

Which one of the following is an array returned by the pseudocode and is it a correct solution?

- A. [50, 20, 10, 5, 1]; the solution is correct
- B. [50, 50, 50, 20, 5]; the solution is correct
- C. [50, 20, 10, 5, 1]; the solution is incorrect
- D. [50, 50, 50, 20, 5]; the solution is incorrect

**Question 2**

Hilbert’s decision problem asks for an algorithm that takes as input a statement of first-order predicate logic and determines whether that statement

- A. is universally valid.
- B. is algorithmically complete.
- C. results in the algorithm returning ‘yes’.
- D. considers only sets and subsets of natural numbers.

**Question 3**

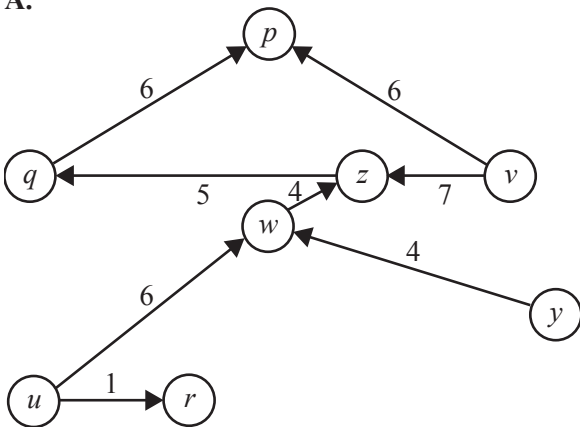
The relationship that Big-O, Big-Ω and Big-Θ notations have with each other is

- A.  $\Theta(f(n))$  necessarily implies  $\Omega(f(n))$  but not  $O(f(n))$ .
- B.  $O(f(n))$  necessarily implies  $\Omega(f(n))$  but not  $\Theta(f(n))$ .
- C.  $O(f(n))$  necessarily implies  $\Theta(f(n))$  and also  $\Omega(f(n))$ .
- D.  $\Theta(f(n))$  necessarily implies  $\Omega(f(n))$  and also  $O(f(n))$ .

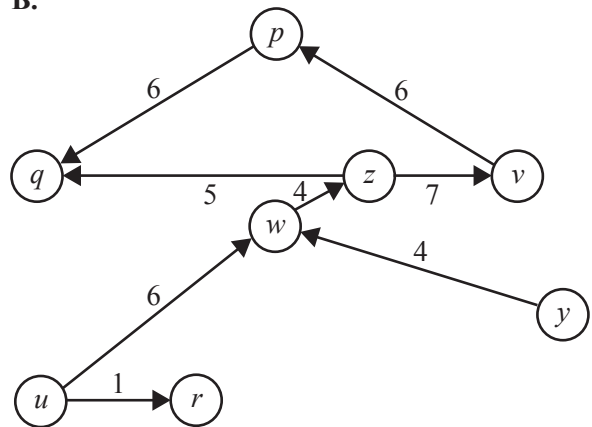
**Question 4**

Which one of the graphs below is a directed acyclic graph with a topological distance between  $u$  and  $v$  that is equal to 17?

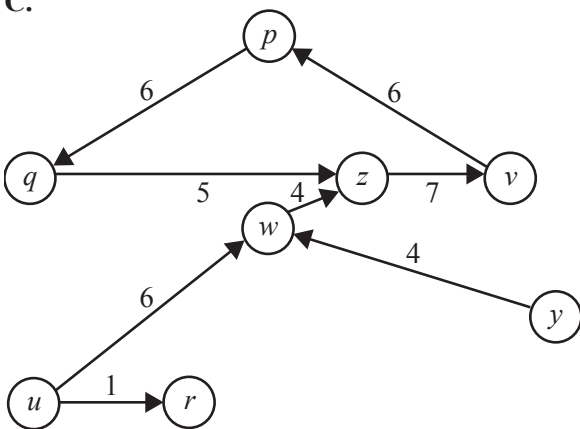
A.



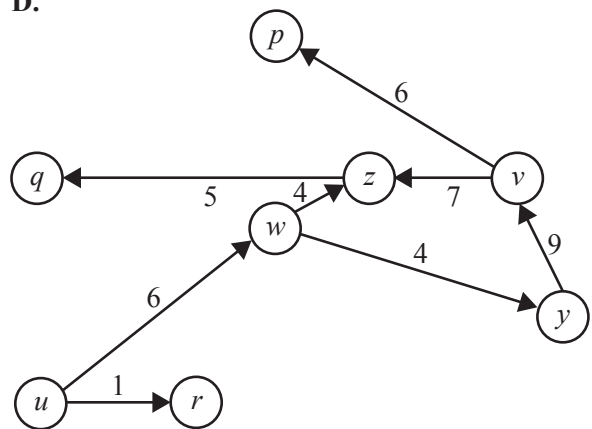
B.



C.



D.



**Question 5**

A proof by contradiction works on the basis of what logical conclusion?

- A. If an assertion is false, its contradiction must be true.
- B. If an assertion is contradictory, its opposite must be true.
- C. If an assertion necessarily leads to a contradiction, the assertion itself is false.
- D. If an assertion necessarily contradicts itself, then the statement has been proven.

**Question 6**

Consider the BinarySearch algorithm executed on an array consisting of the first 10 numbers of the Fibonacci sequence, where  $F_0 = 0$ ,  $F_1 = 1$ ,  $F_2 = 1$ , and so on.

Algorithm searchFib

Input: An array  $A = [F_0, F_1, F_2, \dots, F_9]$ , a target  $x$

Output:  $n$  where  $x = F_n$  if target  $x$  is in  $A$ ,  $-1$  otherwise

low = 0

high = 9

while low  $\leq$  high

    mid = ( low + high )/2 rounded down

    if  $A[\text{mid}] > x$

        high = mid - 1

    else if  $A[\text{mid}] < x$

        low = mid + 1

    else

        return mid

    endif

endwhile

return -1

For which values of  $x$  would the algorithm above finish in a best case running time and a worst case running time, respectively?

- A.  $x = 3, x = 100$
- B.  $x = 5, x = 100$
- C.  $x = 5, x = 34$
- D.  $x = 0, x = 0$

## SECTION B

### Question 1 (4 marks)

Bernie is a professional computer gamer who competes against other players around the world in gaming competitions. Every time he plays against a competitor, he documents information about how they play and how well they do, and stores this information in a file, using the competitor's unique gamer name as the filename. Each file contains information on a single player, such as play styles, win and loss rates, and optimal conditions for successful play.

Bernie has been playing in competitions for a very long time and he now has more than 50 000 separate files documenting the players he has competed against in the past.

Bernie's computer does not have in-built functions for searching folders or files. He would like to be able to search a folder for a file matching a gamer's name so he can quickly look up a player and view or add to the information he has collected on this player. He plans to use binary search to do this, but must first sort the files in alphabetical order for binary search to work.

Explain how a sorting solution using a divide and conquer algorithm design pattern would allow Bernie to efficiently sort the players' filenames.

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### Question 2 (3 marks)

Distinguish between time complexity and space complexity. Use an example as part of your response.

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**Question 3** (4 marks)

Cobham's thesis asserts that only tractable computational problems can be computed on a computational device.

Discuss the limitations of this assertion in relation to practical feasibility.

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**Question 4** (7 marks)

A word is described as ‘alphabetically distant’ if, when all its letters are rearranged in alphabetical order, no two neighbouring letters are also neighbouring in the alphabet. Repeated letters are also considered neighbouring. Some examples are provided below:

- ‘shape’ is alphabetically distant as ‘aehps’ does not have any two neighbouring letters that are also neighbouring in the alphabet.
- ‘algorithm’ is not alphabetically distant as ‘aghilmort’ has three pairs of letters that are neighbouring in the alphabet (‘gh’, ‘hi’, ‘lm’).
- ‘program’ is not alphabetically distant as ‘agmoprr’ has a repeated letter (‘rr’).
- ‘maze’ is alphabetically distant as ‘aemz’ does not have any two neighbouring letters.  
(Note that ‘az’ is not considered neighbouring.)

Jasmine has been tasked with designing an algorithm that scans a given text to find the longest alphabetically distant word. To make the task easier, she has been given all of the words in the text as arrays containing their letters’ positions in the alphabet, sorted in ascending order. For example, ‘shape’ is given as [1, 5, 8, 16, 19], where the first element has an index of 0. Jasmine has designed the following algorithm.

Algorithm AlphaDistant

Input: text, list containing n arrays each representing a single word as integers, sorted ascending  
Output: integer, the length of the longest alphabetically distant word

```

Let longestword = 0
for word in text
    for i = 0 to length of word - 1
        if word[i] = word[i+1] or word[i] - word[i+1] = 1
            return FALSE
        else
            if length of word > longestword
                Let longestword = length of word
            endif
        endif
    endfor
endfor
return longestword

```

- a. Annotate Jasmine’s algorithm above to describe **three** errors present in her attempt. 3 marks
- b. Rewrite Jasmine’s algorithm so that it will correctly solve the errors. 4 marks

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**Question 5** (2 marks)

Explain why, when demonstrating the correctness of an algorithm by induction, it is not sufficient to simply demonstrate that the inductive step holds.

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**Question 6** (8 marks)

An  $n$  metre long roll of silk fabric is to be cut and sold. The value of each sheet of fabric is dependent on its length. The table below provides the values for the three smallest possible lengths, but all values for each length between 1 and  $n$  are known.

Length of sheet of fabric	Value
1 m	\$2.10
2 m	\$3.40
3 m	\$6.55

- a. Outline a greedy heuristic approach to determine how the  $n$  metres of fabric should be cut in order to maximise the total value of the fabric. 4 marks

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- b. Outline a randomised heuristic approach to determine how the  $n$  metres of fabric should be cut in order to maximise the total value of the fabric. 4 marks

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## Answers to multiple-choice questions

Question	Answer
1	C
2	A
3	D
4	B
5	C
6	A