

# Victorian Certificate of Education 2023

Print exam correction: Q9d., matrix H column, 5th row, '1' changed to '0' Print exam correction: Section B, preamble to Q14d., 3rd sentence, removed 2nd 'of'

Letter

STUDENT NUMBER

## GENERAL MATHEMATICS Written examination 2

### Monday 30 October 2023

Reading time: 2.00 pm to 2.15 pm (15 minutes) Writing time: 2.15 pm to 3.45 pm (1 hour 30 minutes)

## **QUESTION AND ANSWER BOOK**

#### Structure of book

| Number of questions | Number of questions<br>to be answered | Number of<br>marks |
|---------------------|---------------------------------------|--------------------|
| 14                  | 14                                    | 60<br>Total 60     |
|                     | 0                                     |                    |

- Students are permitted to bring into the examination room: pens, pencils, highlighters, erasers, sharpeners, rulers, one bound reference, one approved technology (calculator or software) and, if desired, one scientific calculator. Calculator memory DOES NOT need to be cleared. For approved computer-based CAS, full functionality may be used.
- Students are NOT permitted to bring into the examination room: blank sheets of paper and/or correction fluid/tape.

#### **Materials supplied**

- Question and answer book of 25 pages
- Formula sheet
- Working space is provided throughout the book.

#### Instructions

- Write your student number in the space provided above on this page.
- Unless otherwise indicated, the diagrams in this book are **not** drawn to scale.
- All written responses must be in English.

#### At the end of the examination

• You may keep the formula sheet.

Students are NOT permitted to bring mobile phones and/or any other unauthorised electronic devices into the examination room.

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#### Instructions

Answer **all** questions in the spaces provided.

In all questions where a numerical answer is required, you should only round your answer when instructed to do so.

Unless otherwise indicated, the diagrams in this book are **not** drawn to scale.

#### Data analysis

#### **Question 1** (9 marks)

Data was collected to investigate the use of electronic images to automate the sizing of oysters for sale. The variables in this study were:

- *ID:* identity number of the oyster
- *weight:* weight of the oyster in grams (g)
- *volume:* volume of the oyster in cubic centimetres (cm<sup>3</sup>)
- *image size:* oyster size determined from its electronic image (in megapixels)
- *size:* oyster size when offered for sale: small, medium or large

The data collected for a sample of 15 oysters is displayed in Table 1.

#### Table 1

| ID | Weight<br>(g) | <i>Volume</i> (cm <sup>3</sup> ) | <i>Image size</i><br>(megapixels) | Size   |
|----|---------------|----------------------------------|-----------------------------------|--------|
| 1  | 12.9          | 13.0                             | 5.1                               | large  |
| 2  | 11.4          | 11.7                             | 4.8                               | medium |
| 3  | 17.4          | 17.4                             | 6.5                               | large  |
| 4  | 6.8           | 7.2                              | 2.9                               | small  |
| 5  | 9.6           | 10.1                             | 3.7                               | medium |
| 6  | 15.5          | 15.6                             | 5.7                               | large  |
| 7  | 9.7           | 9.9                              | 4.0                               | small  |
| 8  | 7.0           | 7.5                              | 2.7                               | small  |
| 9  | 12.6          | 12.7                             | 5.5                               | medium |
| 10 | 12.5          | 12.7                             | 5.0                               | medium |
| 11 | 10.1          | 10.5                             | 3.9                               | medium |
| 12 | 10.6          | 10.8                             | 4.1                               | medium |
| 13 | 13.0          | 13.1                             | 5.3                               | large  |
| 14 | 8.1           | 8.5                              | 3.5                               | small  |
| 15 | 14.1          | 14.2                             | 5.3                               | large  |

Data: http://jse.amstat.org/jse\_data\_archive.htm

**a.** Write down the number of categorical variables in Table 1.

1 mark

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Question 1 – continued

| b. | Determine, in grams:  |         |
|----|---|---------|
|    | i. the mean <i>weight</i> of all the oysters in this sample   | 1 mark  |
|    |   |         |
|    | mean =  |         |
|    | ii. the median <i>weight</i> of the large oysters in this sample.   | 1 mark  |
|    |   |         |
|    | median =  |         |
| c. | When a least squares line is used to model the association between oyster <i>weight</i> and <i>volume</i> , the equation is:  |         |
|    | $volume = 0.780 + 0.953 \times weight$  |         |
|    | i. Name the response variable in this equation.   | 1 mark  |
|    |   |         |
|    | ii. Complete the following sentence by filling in the box provided.   | 1 mark  |
|    | This equation predicts that, on average, each 10 g increase in the <i>weight</i> of an oyster is associated   |         |
|    |   |         |
|    | with a $cm^3$ increase in its <i>volume</i> .   |         |
| d. | A least squares line can also be used to model the association between an oyster's <i>volume</i> , in cm <sup>3</sup> , and its electronic <i>image size</i> , in megapixels. In this model, <i>image size</i> is the explanatory variable. |         |
|    | Using data from Table 1, determine the equation of this least squares line. Use the template below to write your answer. Round the values of the intercept and slope to four significant figures.   | 2 marks |
|    |   |         |
|    |   |         |
| e. | The number of megapixels needed to construct an accurate electronic image of an oyster is approximately normally distributed.   |         |
|    | Measurements made on recently harvested oysters showed that:  |         |
|    | <ul> <li>97.5% of the electronic images contain less than 4.6 megapixels</li> <li>84% of the electronic images contain more than 4.3 megapixels.</li> </ul>   |         |
|    | Use the 68–95–99.7% rule to determine, in megapixels, the mean and standard deviation of this   |         |
|    | normal distribution.  | 2 marks |
|    | mean = standard deviation =   |         |
|    |   |         |
|    |   |         |

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#### Question 2 (5 marks)

**a.** The following data shows the sizes of a sample of 20 oysters rated as small, medium or large.

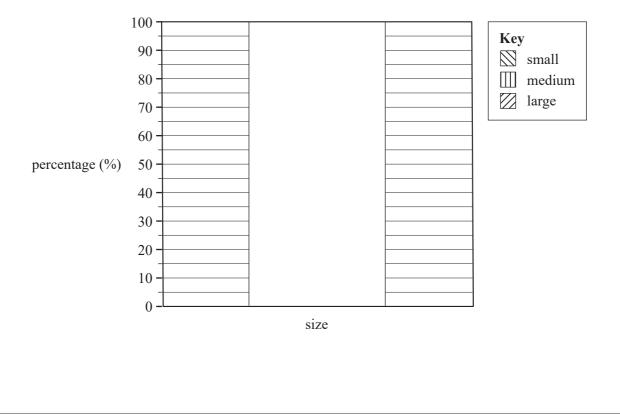
| small  | small  | large  | medium | medium |
|--------|--------|--------|--------|--------|
| medium | large  | small  | medium | medium |
| small  | medium | small  | small  | medium |
| medium | medium | medium | small  | large  |

i. Use the data above to complete the following frequency table.

#### Table 2

|        | Frequency |                |  |  |  |
|--------|-----------|----------------|--|--|--|
| Size   | Number    | Percentage (%) |  |  |  |
| small  |           | 35             |  |  |  |
| medium |           | 50             |  |  |  |
| large  |           | 15             |  |  |  |
| Total  |           | 100            |  |  |  |

**ii.** Use the percentages in Table 2 to construct a percentage segmented bar chart below. A key has been provided.



AREA

Question 2 – continued

1 mark

An oyster farmer has two farms, A and B.

She takes a random sample of oysters from each of the farms and has the oysters classified as small, medium or large.

The number of oysters of each size is displayed in the two-way table below.

| Table 3 |  | 3 |
|---------|--|---|
|---------|--|---|

| Oyster size | Farm A | Farm B |
|-------------|--------|--------|
| small       | 42     | 114    |
| medium      | 124    | 160    |
| large       | 44     | 46     |
| Total       | 210    | 320    |

**b. i.** Calculate the percentage of the total number of oysters graded as 'large' in this investigation. Round the percentage to the nearest whole number.

1 mark

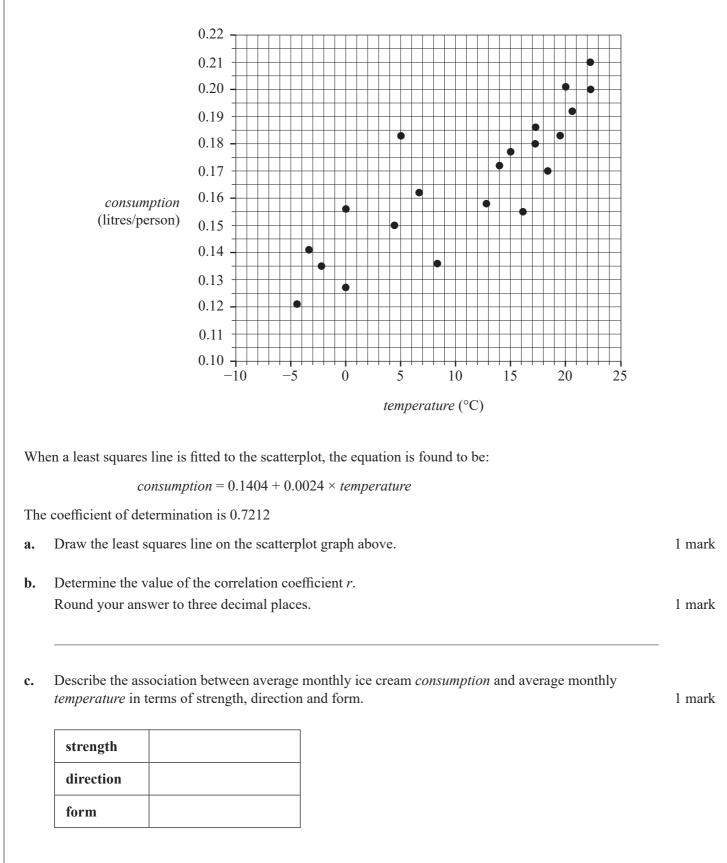
**ii.** The farmer believes that farm A has a greater capacity to grow larger oysters than farm B. Does the information in Table 3 support the farmer's belief? Explain your conclusion by comparing the values of two appropriate percentages.

Round these percentages to the nearest whole number.

2 marks

#### **Question 3** (6 marks)

The scatterplot below plots the average monthly ice cream *consumption*, in litres/person, against average monthly *temperature*, in °C. The data for the graph was recorded in the Northern Hemisphere.



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 $Question \ 3-\text{continued}$ 

| variables <i>consumption</i> and <i>temperature</i> .  | 1 |
|--|---|
| Use the equation of the least squares line to predict the average monthly ice cream <i>consumption</i> , in litres per person, when the monthly average <i>temperature</i> is $-6$ °C. | 1 |
| Write down whether this prediction is an interpolation or an extrapolation.  | 1 |
|  |   |
|  |   |
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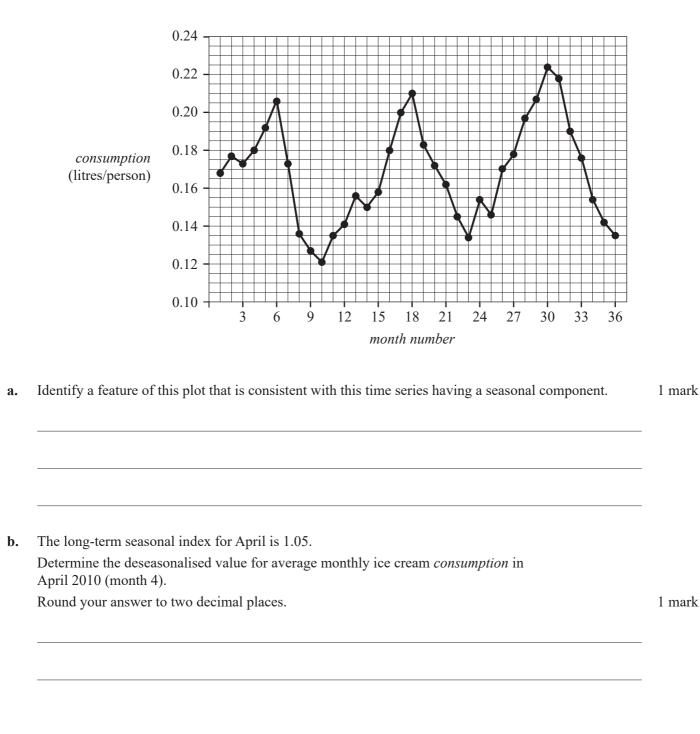
7

#### Question 4 (4 marks)

The time series plot below shows the average monthly ice cream *consumption* recorded over three years, from January 2010 to December 2012.

The data for the graph was recorded in the Northern Hemisphere.

In this graph, month number 1 is January 2010, month number 2 is February 2010 and so on.



Question 4 – continued

c. Table 4 below shows the average monthly ice cream *consumption* for 2011.

| Table | 4 |
|-------|---|
|-------|---|

|      |       |       |       | С     | onsumpt | <i>tion</i> (litr | es/perso | n)    |       |       |       |       |
|------|-------|-------|-------|-------|---------|-------------------|----------|-------|-------|-------|-------|-------|
| Year | Jan   | Feb   | Mar   | Apr   | May     | Jun               | Jul      | Aug   | Sep   | Oct   | Nov   | Dec   |
| 2011 | 0.156 | 0.150 | 0.158 | 0.180 | 0.200   | 0.210             | 0.183    | 0.172 | 0.162 | 0.145 | 0.134 | 0.154 |

Show that, when rounded to two decimal places, the seasonal index for July 2011 estimated from this data is 1.10. 2 marks

| 23 GEI      | NMATH 2 10  |        |
|-------------|---|--------|
| Re          | cursion and financial modelling   |        |
| Art<br>Inte | estion 5 (3 marks)<br>hur borrowed \$30000 to buy a new motorcycle.<br>erest on this loan is charged at the rate of 6.4% per annum, compounding quarterly.<br>hur will repay the loan in full with quarterly repayments over six years. |        |
| a.          | How many repayments, in total, will Arthur make?  | 1 mark |
| The         | e balance of the loan, in dollars, after <i>n</i> quarters, $A_n$ , can be modelled by the recurrence relation<br>$A_0 = 30000, \qquad A_{n+1} = 1.016A_n - 1515.18$  |        |
| b.          | Showing recursive calculations, determine the balance of the loan after two quarters.<br>Round your answer to the nearest cent.   | 1 mark |
|             |   |        |
| c.          | The final repayment required will differ slightly from all the earlier repayments of \$1515.18  |        |
|             | Determine the value of the final repayment.<br>Round your answer to the nearest cent.   | 1 mark |
|             |   |        |
|             |   |        |
|             |   |        |
|             |   |        |
|             |   |        |

#### Question 6 (4 marks)

Arthur invests \$600000 in an annuity that provides him with a monthly payment of \$3973.00 Interest is calculated monthly.

Three lines of the amortisation table for this annuity are shown below.

| Payment<br>number | Payment<br>(\$) | Interest<br>(\$) | Principal reduction<br>(\$) | Balance<br>(\$) |
|-------------------|-----------------|------------------|-----------------------------|-----------------|
| 0                 | 0.00            | 0.00             | 0.00                        | 600 000.00      |
| 1                 | 3973.00         | 2520.00          | 1453.00                     | 598 547.00      |
| 2                 | 3973.00         | 2513.90          | 1459.10                     | 597087.90       |

**a.** The interest rate for the annuity is 0.42% per month.

Determine the interest rate per annum.

b. Using the values in the table, complete the next line of the amortisation table.Write your answers in the spaces provided in the table below.Round all values to the nearest cent.

| Payment<br>number | Payment<br>(\$) | Interest<br>(\$) | Principal reduction<br>(\$) | Balance<br>(\$) |
|-------------------|-----------------|------------------|-----------------------------|-----------------|
| 0                 | 0.00            | 0.00             | 0.00                        | 600 000.00      |
| 1                 | 3973.00         | 2520.00          | 1453.00                     | 598 547.00      |
| 2                 | 3973.00         | 2513.90          | 1459.10                     | 597087.90       |
| 3                 |                 |                  |                             |                 |

**c.** Let  $V_n$  be the balance of Arthur's annuity, in dollars, after *n* months.

Write a recurrence relation in terms of  $V_0$ ,  $V_{n+1}$  and  $V_n$  that can model the value of the annuity from month to month.

1 mark

1 mark

Question 6 – continued

| d. | The amortisation tables on page 11 show that the balance of the annuity reduces each month.                           |     |
|----|---|-----|
|    | If the balance of an annuity remained constant from month to month, what name would be given to this type of annuity? | 1 r |

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| nterest on this loan compounds weekly.  |   |        |  |  |  |  |  |  |
|---|---|--------|--|--|--|--|--|--|
| he balance of the loan, in dollars, after $n$ weeks, $V_n$ , can be determined using a recurrence relation of the orm |   |        |  |  |  |  |  |  |
|   | $V_0 = 60000, \qquad V_{n+1} = 1.0015V_n - d$   |        |  |  |  |  |  |  |
| •   | Show that the interest rate for this loan is 7.8% per annum.  |        |  |  |  |  |  |  |
|   | Determine the value of <i>d</i> in the recurrence relation if   |        |  |  |  |  |  |  |
|   | i. Arthur makes interest-only repayments  | 1 mark |  |  |  |  |  |  |
|   | ii. Arthur fully repays the loan in five years.   |        |  |  |  |  |  |  |
|   | Round your answer to the nearest cent.  | 1 mark |  |  |  |  |  |  |
|   | Arthur decides that the value of $d$ will be 300 for the first year of repayments.  |        |  |  |  |  |  |  |
|   | If Arthur fully repays the loan with exactly three more years of repayments, what new value of <i>d</i> will apply for these three years? |        |  |  |  |  |  |  |
|   | Round your answer to the nearest cent.  | 1 mark |  |  |  |  |  |  |
|   |   |        |  |  |  |  |  |  |
| •   | For what value of $d$ does the recurrence relation generate a geometric sequence?   | 1 mark |  |  |  |  |  |  |
|   |   |        |  |  |  |  |  |  |
|   |   |        |  |  |  |  |  |  |
|   |   |        |  |  |  |  |  |  |

#### Matrices

#### Question 8 (3 marks)

A circus sells three different types of tickets: family (F), adult (A) and child (C). The cost of admission, in dollars, for each ticket type is presented in matrix N below.

$$N = \begin{bmatrix} 36\\15\\8\end{bmatrix} C$$

The element in row *i* and column *j* of matrix *N* is  $n_{ij}$ .

**a.** Which element shows the cost for one child ticket?

b. A family ticket will allow admission for two adults and two children.

Complete the matrix equation below to show that purchasing a family ticket could give families a saving of \$10.

 $\begin{bmatrix} 0 & 2 & 2 \end{bmatrix} \times N - \begin{bmatrix} \dots & \dots & \dots \end{bmatrix} \times N = \begin{bmatrix} 10 \end{bmatrix}$ 

c. On the opening night, the circus sold 204 family tickets, 162 adult tickets and 176 child tickets.
 The owners of the circus want a 3 × 1 product matrix that displays the revenue for each ticket type: family, adult and child.

This product matrix can be achieved by completing the following matrix multiplication.

$$K \times N = \begin{bmatrix} 7344\\2430\\1408 \end{bmatrix}$$

Write down matrix *K* in the space below.

K =

#### Question 9 (4 marks)

The circus is held at five different locations, E, F, G, H and I.

The table below shows the total revenue for the ticket sales, rounded to the nearest hundred dollars, for the last 20 performances held at each of the five locations.

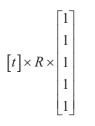
| Location     | E         | F         | G        | Н        | Ι         |
|--------------|-----------|-----------|----------|----------|-----------|
| Ticket sales | \$960 000 | \$990 500 | \$940100 | \$920800 | \$901 300 |

The ticket sales information is presented in matrix R below.

 $R = \begin{bmatrix} 960\ 000 & 990\ 500 & 940\ 100 & 920\ 800 & 901\ 300 \end{bmatrix}$ 

a. Complete the matrix equation below that calculates the average ticket sales per performance at each of the five locations.
 1 mark

The circus would like to increase its total revenue from the ticket sales from all five locations. The circus will use the following matrix calculation to target the next 20 performances.



**b.** Determine the value of *t* if the circus would like to increase its revenue from ticket sales by 25%.

The circus moves from one location to the next each month. It rotates through each of the five locations, before starting the cycle again.

The following matrix displays the movement between the five locations.

#### **c.** The circus started in town *I*.

What is the order in which the circus will visit the five towns?

The circus plans to add a sixth location, J.

The only change to the cycle is that the circus will be held at location J after location E and before location G.

**d.** Complete the three columns in the following matrix, showing the new movement between the six locations, *E*, *F*, *G*, *H*, *I* and *J*.

1 mark

1 mark

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0 0

this month G H IΕ FJ\_\_\_\_\_0 \_\_\_\_\_1 0 E \_\_\_\_\_0 \_\_\_\_\_0 \_\_\_\_\_ F\_\_\_\_\_0 \_\_\_\_\_0 \_\_\_0 G next month \_\_\_\_ 0 \_\_\_\_ 0 \_1 \_\_\_ *H* \_\_\_\_ 1 \_\_\_\_ 0 0 \_\_\_ *I*  $\_ 0 \_ 0 0 \_ ]J$ 

#### Question 10 (3 marks)

Within the circus, there are different types of employees: directors (D), managers (M), performers (P) and sales staff (S). Customers (C) attend the circus.

Communication between the five groups depends on whether they are customers or employees, and on what type of employee they are.

Matrix *G* below shows the communication links between the five groups.

|            | receiver |   |   |   |   |   |  |
|------------|----------|---|---|---|---|---|--|
|            |          |   | M |   |   |   |  |
| G = sender | D        | 0 | 1 | 1 | 1 | 1 |  |
|            | M        | 1 | 0 | 1 | 1 | 1 |  |
| G = sender | P        | 0 | 1 | 0 | 0 | 0 |  |
|            | S        | 0 | 1 | 0 | 0 | 1 |  |
|            | С        | 0 | 0 | 0 | 1 | 0 |  |

In this matrix:

- The '1' in row D, column M indicates that the directors can communicate directly with the managers.
- The '0' in row *P*, column *D* indicates that the performers cannot communicate directly with the directors.
- **a.** A customer wants to make a complaint to a director.

What is the shortest communication sequence that will successfully get this complaint to a director? 1 mark

**b.** Matrix *H* below shows the number of two-step communication links between each group. Sixteen elements in this matrix are missing.

 $H = sender \begin{array}{ccccc} D & M & P & S & C \\ D & 1 & --- & --- \\ M & 0 & --- & --- \\ M & 0 & --- & --- \\ 1 & --- & --- \\ S & 1 & --- & --- \\ C & 0 & 1 & 0 & 0 & 1 \end{array}$ 

- i. Complete matrix *H* above by filling in the missing elements.
- ii. What information do elements  $g_{21}$  and  $h_{21}$  provide about the communication between the circus employees?

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1 mark

#### Question 11 (2 marks)

The circus requires 180 workers to put on each show.

From one show to the next, workers can either continue working (W) or they can leave the circus (L).

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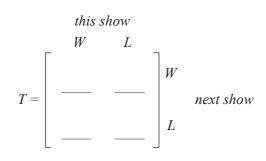
Once workers leave the circus, they do not return.

It is known that 95% of the workers continue working at the circus.

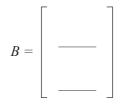
This situation can be modelled by the matrix recurrence relation

$$S_0 = \begin{bmatrix} 180\\0 \end{bmatrix}, \qquad S_{n+1} = TS_n + B$$

**a.** Write down matrix *T*, the transition matrix, for this recurrence relation.



**b.** Write down matrix *B* for this recurrence relation to ensure that the circus always has 180 workers. 1 mark

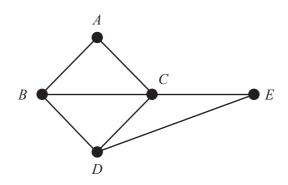


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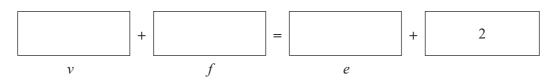
#### Networks and decision mathematics

#### Question 12 (4 marks)

A country has five states, *A*, *B*, *C*, *D* and *E*. A graph can be drawn with vertices to represent each of the states. Edges represent a border shared between two states.



- **a.** What is the sum of the degrees of the vertices of the graph above?
- **b.** Euler's formula, v + f = e + 2, holds for this graph.
  - i. Complete the formula by writing the appropriate numbers in the boxes provided below. 1 mark



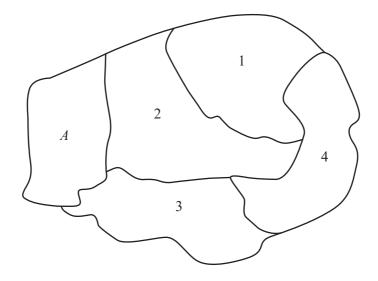
**ii.** Complete the sentence by writing the appropriate word in the box provided below.

Euler's formula holds for this graph because the graph is connected and

Question 12 – continued

1 mark

**c.** The diagram below shows the position of state *A* on a map of this country. The four other states are indicated on the diagram as 1, 2, 3 and 4.



Use the information in the graph on page 20 to complete the table below. Match the state (B, C, D and E) with the corresponding state number (1, 2, 3 and 4) given in the map above. 1 mark

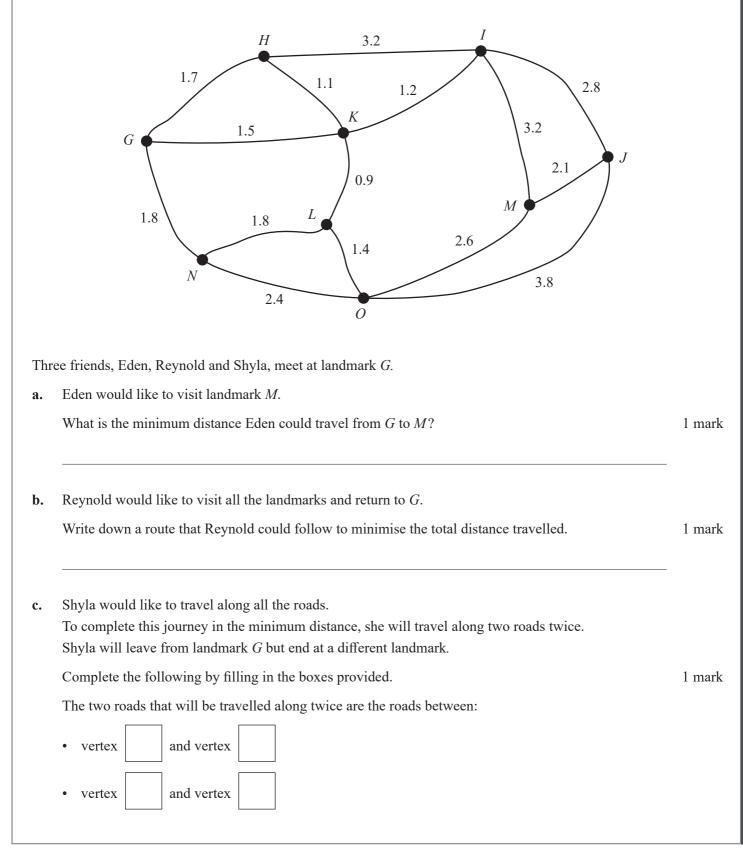
| State | State number |
|-------|--------------|
| В     |              |
| С     |              |
| D     |              |
| Е     |              |

#### Question 13 (3 marks)

The state A has nine landmarks, G, H, I, J, K, L, M, N and O.

The edges on the graph represent the roads between the landmarks.

The numbers on each edge represent the length, in kilometres, along each road.

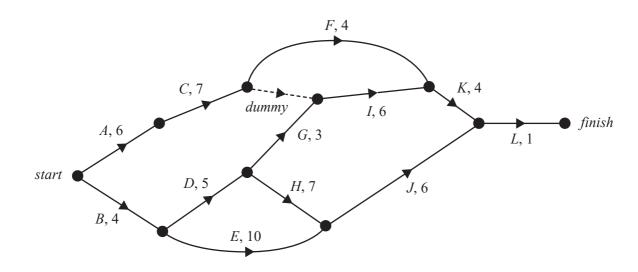


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#### Question 14 (5 marks)

One of the landmarks in state A requires a renovation project.

This project involves 12 activities, A to L. The directed network below shows these activities and their completion times, in days.



The table below shows the 12 activities that need to be completed for the renovation project. It also shows the earliest start time (EST), the duration, and the immediate predecessors for the activities. The immediate predecessor(s) for activity I and the EST for activity J are missing.

| Activity | EST | Duration | Immediate<br>predecessor(s) |
|----------|-----|----------|-----------------------------|
| Α        | 0   | 6        | _                           |
| В        | 0   | 4        | _                           |
| С        | 6   | 7        | A                           |
| D        | 4   | 5        | В                           |
| Е        | 4   | 10       | В                           |
| F        | 13  | 4        | С                           |
| G        | 9   | 3        | D                           |
| Н        | 9   | 7        | D                           |
| Ι        | 13  | 6        |                             |
| J        |     | 6        | E, H                        |
| K        | 19  | 4        | <i>F, I</i>                 |
| L        | 23  | 1        | J, K                        |

 $Question \ 14-continued$ 

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| l <b>.</b> | Write down the immediate predecessor(s) for activity <i>I</i> .  |   |  |   |   |                               | 1                           |              |
|------------|--|---|--|---|---|-------------------------------|-----------------------------|--------------|
| •          | What is the earliest start time, in days, for activity $J$ ?   |   |  |   |   |                               | 1                           |              |
|            | How many activities have a float time of zero?   |   |  |   |   |                               | 1                           |              |
| hes        | managers of the se reductions we maximum dec   | vill result in a  | n increase in  | the cost of co  | ompleting the                                     |                               |                             |              |
| A          | ctivity  | A   | В  | F   | Н   | Ι                             | K                           |              |
| D          | aily cost (\$)   | 1500  | 2000   | 2500  | 1000  | 1500                          | 3000                        |              |
| l <b>.</b> | If activities <i>A</i> of the project<br>What will be  | will be reduc   | ed.  |   | ced by two da                                     | ays each, the                 | overall completi            | on time<br>1 |
|            | of the project<br>What will be<br><br>The managers<br>activities to p  | will be reduc<br>the maximum<br>s of the project<br>roduce the ma<br>table below, s                                       | ed.<br>a reduction ti<br>et have a max<br>aximum redu<br>showing the   | me, in days?<br>kimum budge<br>action in the p<br>reductions in                               | t of \$15000 t<br>roject's overa<br>individual ac | o reduce the<br>all completio | time for several            | 1            |
| -          | of the project<br>What will be<br>The managers<br>activities to p<br>Complete the  | will be reduc<br>the maximum<br>s of the project<br>roduce the ma<br>table below, s<br>arliest comple<br><b>Reduction</b> | ed.<br>a reduction ti<br>et have a max<br>aximum redu<br>showing the   | me, in days?<br>kimum budge<br>action in the p<br>reductions in<br>thin the \$150<br>ion time | t of \$15000 t<br>roject's overa<br>individual ac | o reduce the<br>all completio | time for several<br>n time. | 1<br>        |
|            | of the project<br>What will be<br>The managers<br>activities to p<br>Complete the<br>achieve the ea                            | will be reduc<br>the maximum<br>s of the project<br>roduce the ma<br>table below, s<br>arliest comple<br><b>Reduction</b> | ed.<br>reduction ti<br>a reduction ti<br>thave a max<br>aximum reduction<br>showing the<br>tion time with<br><b>i in complet</b> | me, in days?<br>kimum budge<br>action in the p<br>reductions in<br>thin the \$150<br>ion time | t of \$15000 t<br>roject's overa<br>individual ac | o reduce the<br>all completio | time for several<br>n time. | 1<br>        |
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| -          | of the project<br>What will be<br>The managers<br>activities to p<br>Complete the<br>achieve the ea<br>Activity<br>A           | will be reduc<br>the maximum<br>s of the project<br>roduce the ma<br>table below, s<br>arliest comple<br><b>Reduction</b> | ed.<br>reduction ti<br>a reduction ti<br>thave a max<br>aximum reduction<br>showing the<br>tion time with<br><b>i in complet</b> | me, in days?<br>kimum budge<br>action in the p<br>reductions in<br>thin the \$150<br>ion time | t of \$15000 t<br>roject's overa<br>individual ac | o reduce the<br>all completio | time for several<br>n time. | 1<br>        |
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| I.         | of the project<br>What will be<br>The managers<br>activities to p<br>Complete the<br>achieve the ea<br>Activity<br>A<br>B<br>F | will be reduc<br>the maximum<br>s of the project<br>roduce the ma<br>table below, s<br>arliest comple<br><b>Reduction</b> | ed.<br>reduction ti<br>a reduction ti<br>thave a max<br>aximum reduction<br>showing the<br>tion time with<br><b>i in complet</b> | me, in days?<br>kimum budge<br>action in the p<br>reductions in<br>thin the \$150<br>ion time | t of \$15000 t<br>roject's overa<br>individual ac | o reduce the<br>all completio | time for several<br>n time. | 1<br>        |

## END OF QUESTION AND ANSWER BOOK



Victorian Certificate of Education 2023

## **GENERAL MATHEMATICS**

## Written examination 2

FORMULA SHEET

Instructions

This formula sheet is provided for your reference. A question and answer book is provided with this formula sheet.

Students are NOT permitted to bring mobile phones and/or any other unauthorised electronic devices into the examination room.

## **General Mathematics formulas**

## Data analysis

| standardised score                 | $z = \frac{x - \overline{x}}{s_x}$  |
|------------------------------------|---|
| lower and upper fence in a boxplot | lower $Q1 - 1.5 \times IQR$ upper $Q3 + 1.5 \times IQR$                             |
| least squares line of best fit     | $y = a + bx$ , where $b = r \frac{s_y}{s_x}$ and $a = \overline{y} - b\overline{x}$ |
| residual value                     | residual value = actual value – predicted value                                     |
| seasonal index                     | seasonal index = $\frac{\text{actual figure}}{\text{deseasonalised figure}}$        |

## Recursion and financial modelling

| first-order linear recurrence relation                                | $u_0 = a, \qquad u_{n+1} = Ru_n + d$  |
|---|---|
| effective rate of interest for a compound interest loan or investment | $r_{effective} = \left[ \left( 1 + \frac{r}{100n} \right)^n - 1 \right] \times 100\%$ |

#### Matrices

| determinant of a $2 \times 2$ matrix | $A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}, \qquad \det A = \begin{vmatrix} a & b \\ c & d \end{vmatrix} = ad - bc$ |
|--------------------------------------|--|
| inverse of a $2 \times 2$ matrix     | $A^{-1} = \frac{1}{\det A} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$ , where $\det A \neq 0$                         |
| recurrence relation                  | $S_0 = \text{initial state}, \qquad S_{n+1} = T S_n + B$   |
| Leslie matrix recurrence relation    | $S_0 = \text{initial state}, \qquad S_{n+1} = L S_n$   |

### Networks and decision mathematics

| Euler's formula | v + f = e + 2 |
|-----------------|---------------|
|-----------------|---------------|